

**Programme Outcomes, Programme Specific  
Outcomes and Course Outcomes  
for  
Ph.D. Programs**

**Program Name: Ph.D. in Mathematics**



Department of Mathematics  
**University of North Bengal**

West Bengal, INDIA

### **Program Outcomes**

- Developing skills to critically examine the background literature relevant to their specific research area.
- To prepare students for a career in research and teaching at college and university level.
- To prepare students for professions other than teaching, that requires independent mathematical research, advanced mathematical knowledge, critical analysis and thoughtful synthesis.
- The opportunity to expand the student's knowledge of their research area, including its theoretical foundations and the specific techniques used to study it.

### **Program Specific Outcomes**

- Thorough knowledge of the literature and a comprehensive understanding of scientific methods and techniques applicable to their own research.
- Be able to act autonomously in the planning and implementation of research.
- Be able to communicate complex ideas effectively both verbally and in writing, which includes the ability to write their Ph.D. thesis, give presentation at various conferences and to submit a research paper or article to a journal for publication.

<b>Paper Code</b>	<b>Unit Title</b>	<b>Marks</b>	<b>Credits</b>
<b>PCWMATH 1</b>	Research Methodology Unit -1: Research Foundation	50	2
	Research Methodology Unit -2: Mathematical Typesetting as a Computer Applications in Research	50	2
<b>PCWMATH 2</b>	T: Theory of Convergence and Topological Hyperalgebra	50	2
	C: Theory of Entire and Meromorphic Functions	50	2
	M: Measure Theory	50	2
	A: Algebra	50	2
	N: Number Theory	50	2

**Ph.D. Course Work  
(Mathematics)**

Paper Code	Unit Title	Course Outcomes
PCWMATH 1	Research Methodology Unit -1: Research Foundation	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Basic introduction of methodology used in research in general and mathematical science in particular.</li> <li>• Identification of research problems and sub-problems.</li> <li>• Different technique of interpretation.</li> <li>• Ethical issues and professional conduct.</li> <li>• Literature review</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Ability to learn criteria of good research.</li> <li>• Defining techniques involved in different problems.</li> <li>• Understanding characteristics of research documentations (reviews, treatise, monographs, technical report, white paper, thesis, research paper.)</li> <li>• Techniques of writing project proposals, paper presentation, and soft skills.</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Professional ethics, ethical issues and their significance those arises from computer technology.</li> <li>• Concept of ethical issues related to plagiarism and intellectual property rights.</li> <li>• Importance of different issues in defining a research problem including literature in research proposal, critique, survey and pre-review process.</li> <li>• Identifying gaps areas from literature review.</li> </ul>
PCWMATH 1	Research Methodology Unit -2: Mathematical Typesetting as a Computer Applications inResearch	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Use of various document classes for example: article.cls, book.cls</li> <li>• Use of different packages like amssymb,amsmath,amsfonts,graphics.</li> <li>• Paper /article writing by using Latex which are compatible with almost all mathematical journals (MatSciNet, Scopus, Taylor Francis, Springer etc.)</li> <li>• Preparing presentation using beamer</li> </ul> <p>Skill gained:</p> <ul style="list-style-type: none"> <li>• Ability for framing preamble according to desired looks of presentation.</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Ability for further use of new softwares towards making good documents.</li> </ul>
PCWMATH 2 (T)	Theory of Convergence and Topological Hyperalgebra	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Definition of natural density.</li> <li>• Concept of statistical convergence</li> <li>• Basic properties of statistical convergence.</li> <li>• Concept of <math>I</math> and <math>I^*</math>-convergence.</li> <li>• Concept of <math>I</math>-<math>\lambda</math> statistical convergence.</li> <li>• Concept of topological groups, semigroups and rings.</li> <li>• Definition of topological hyperstructures.</li> <li>• Topological polygroups.</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Comparing the differences between classical convergence and statistical convergence.</li> <li>• Comparing the differences between statistical convergence and <math>I</math>-convergence.</li> <li>• Analyzing the structure of the set of all <math>I</math>-convergent sequence.</li> <li>• Comparing the differences between <math>I</math> and <math>I^*</math>-convergence.</li> <li>• Comparing the differences between topological groups and topological rings.</li> </ul>

		<p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Comparing the differences between basis and Schauder basis.</li> <li>• Ability of applying the concepts of statistical convergence, <math>I</math> and <math>I^*</math>-convergence.</li> <li>• Applications of topology towards extension of the study of topological algebraic hyperstructures.</li> <li>• Computing the isomorphism theorem.</li> </ul>
PCWMATH 2 (C)	Theory of Entire and Meromorphic Functions	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Meromorphic functions, Properties of Nevanlinna's characteristic function.</li> <li>• Growth of meromorphic functions, Comparative growth of functions.</li> <li>• Deficiencies of meromorphic functions.</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Nevanlinna characteristic function is like maximum modulus function for meromorphic functions.</li> <li>• Order of growth of functions.</li> <li>• Relation between maximum modulus function and Nevanlinna characteristic function.</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Explore properties of meromorphic functions with Nevanlinna characteristic function.</li> <li>• Factorization of function in terms of zeros and poles.</li> <li>• Calculation of counting function and proximity function.</li> </ul>
PCWMATH 2 (M)	Measure Theory	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Lebesgue outer measure and Lebesgue measure on Euclidean space.</li> <li>• Borel measure space of n-dimension and its completion</li> <li>• s-dimensional Hausdorff measure on <math>\mathbb{R}^n</math> for <math>s \in [0, \infty)</math> and Hausdorff dimension of a subset of <math>\mathbb{R}^n</math>.</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Ability of constructing Lebesgue outer measure and Lebesgue measure on Euclidean space using covering classes</li> <li>• Estimating Lebesgue measure on <math>\mathbb{R}^n</math> by closed compact sets and approximation by open sets.</li> <li>• Determination of Hausdorff dimension of a set <math>E \subset \mathbb{R}^n</math>.</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Realizing importance of Borel measurability and metric outer measurability in the related theory.</li> <li>• Understanding the role of completion to obtain Lebesgue measure space via Borel measure space in <math>\mathbb{R}^n</math>.</li> <li>• Building a foundation for study Cantor sets, Fractals, etc.</li> </ul>
PCWMATH 2 (A)	Algebra	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Concept of Normal series, Subnormal series, solvable series.</li> <li>• Solvable groups, Nilpotent groups, Torsion group, finitely generated Abelian groups etc.</li> <li>• Noetherian Rings, Artinian Rings etc.</li> <li>• Galois groups, Cyclotomic field extension, Radical extensions, Algebraic independence etc.</li> </ul> <p>Skill gained:</p> <ul style="list-style-type: none"> <li>• Construction of different groups, e.g. solvable groups, nilpotent groups etc.</li> <li>• Solving problems using fundamental theorem of Abelian groups.</li> <li>• Ability to build different Galois groups and Galois fields.</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Ability to study these concepts in different algebraic structures, theories.</li> <li>• Interest as well as capability to study Coding Theory, Cryptography</li> </ul>

		etc.
PCWMATH 2 (N)	Number Theory	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Dirichlet series, multiplication of Dirichlet series.</li> <li>• Riemann zeta function, its functional equation and analytic continuation, its relation with distribution of primes.</li> <li>• Analytic proof of prime number theorem</li> </ul> <p>Skill gained:</p> <ul style="list-style-type: none"> <li>• Finding zero free regions of Riemann zeta function</li> <li>• Ability to understand distribution of primes</li> <li>• Ability to deal with different Dirichlet series.</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Useful tools to deal with various problems in analytic number theory.</li> </ul>